## Science and Technology Education

Document Series No. 35

# Mathematics, Education, and Society

Reports and papers presented in the
Fifth Day Special Programme
on "Mathematics, Education, and Society"
at the 6th International Congress on Mathematical Education
Budapest, 27 July - 3 August, 1988

edited by

Christine Keitel
(Chief editor)
and
Peter Damerow, Alan Bishop, Paulus Gerdes
(Chief organizers)

Division of Science Technical and Environmental Education

**UNESCO** 

#### Table of Contents

Mathematics, Education, and Society (MES)	10S 1
Mathematics Education and Culture	1
Social History of Mathematics Education	1
Arpàd Szabó: Mathematics and Dialectics	2
Ahmed Djebbar: The Content of Mathematics Teaching in North Africa in the Middle Ages	2
and its Role in Present Day Teaching	3
John Fauvel: Should We Bring Back the Mathematical Practitioner? Learning From the Social History of Mathematics Education in the British Renaissance	4
Gert Schubring: Theoretical Categories for Investigations in the Social History of Mathematics Education and Some Characteristic Patterns	6
Cultural Diversity and Conflicts in Mathematics Education	8
Terezinha Nunes Carraher: Material Embodiments of Mathematics Models in Everyday Life	8
Lloyd Dawe: Mathematics Teaching and Learning in Village Schools of the South Pacific	10
Murad Jurdak: Religion and Language as Cultural Carriers and Barriers in Mathematics	
Education P.T. M. Z. L.	12
Claudia Zaslavsky: Integrating Mathematics With the Study of Cultural Traditions	14
The Cultural Role of Mathematics Education in the Future	16
Leone Burton: Mathematics as a Cultural Experience: Whose Experience?	16
Desmond Broomes: The Mathematical Demands of a Rural Economy	19
Kathryn Crawford: Knowing What Versus Knowing How: The Need for a Change in Emphasis for Minority Group Education in Mathematics	22
Philip I Davis: Applied Mathematics as Social Contract	24
Rik Pinxten: World View and Mathematics Teaching	28
Society and Institutionalized Mathematics Education	30
Mathematics as a Cultural Product	30
Jens Høyrup: On Mathematics and War	30
George Ghevarghese Joseph: Eurocentrism in Mathematics: The Historical Dimensions	32
Sam O. Ale: Mathematics in Rural Societies	35
Leo Rogers: The Cultural History of Mathematics as a Basis for Philosophies of Mathematics Education	38
The Image of Mathematics in Society	40
Gilah C. Leder: The Image of Mathematics in Society: A Case Study	40
Stanban Larmon, A Social View of Mathematics Implications for Mathematics	10
Education	42
Chandler Davis: A Hippocratic Oath for Mathematicians?	44

Sociology of Institutionalized Mathematics	47
Eduard Glas: Social Determinants of Mathematical Change: The Ecole Polytechnique 1794–1809	47
Renate Tobies: The Activities of Felix Klein in the Teaching Commission of the 2nd Chamber of the Prussian Parliament	50
Emma Castelnuovo: The Teaching of Geometry in Italian High Schools During the Last Two Centuries: Some Aspects Related to Society	51
the Last Two Centuries: Some Aspects Related to Society  Michael H. Price: Some Reflections on the Role of Associations in Mathematics  Education	52
The Mathematics Curriculum as a Social Issue	54
Michael Otte: "Mathematics for All" and the Epistemological Problems of Mathematics Education	54
Neil Bibby and John Abraham: Social History of Mathematical Controversies: Some Implications for the Curriculum	56
Bernard Charlot: Institutional and Socio-Economic Context of the "Modern Mathematics"	
Reform in France	58
Non-School Alternatives for Mathematics Education	59
John D. Volmink: Non-School Alternatives in Mathematics Education	59
Sixto Romero Sanchez: The Necessity of Popularizing Mathematics via Radio Programs	61
Virginia Thompson: FAMILY MATH: Linking Home and Mathematics	62
Jeffrey T. Evans: Mathematics for Adults: Community Research and the "Barefoot Statistician"	65
The Mathematical Demands of the Economy	
Guida Maria Correia P. de Abreu and David William Carraher: The Mathematics of Brazilian Sugar Cane Farmers	68
Wang Chang Pei: Differences in Mathematics Education Between Rural Area and Urban Area in China	70
Howard Russell: The Generic Skills Economic Development Project: The Mathematical Demands of the Economy	73
Bernhelm Booß-Bavnbek and Glen Pate: Expanding Risk in Technological Society Through Progress in Mathematical Modeling	75
c and institutionalized Mathematics Education	
Mathematics Education Under Different Cultural Constraints	78
Siaka Bamba Kanté: Critical Issues of Mathematics Education in the Ivory Coast	78
Jens Naumann: Practical Aspects of Basic Mathematics Teaching in Senegalese Villages	79
Diana C. Rosenberg: Knowledge Transfer From one Culture to Another: HEWET From the Netherlands to Argentina	82
Munir Fasheh: Mathematics in a Social Context: Math Within Education as Praxis  Versus Within Education as Hegemony	84
Society as a Source of Ideas for Mathematics Teaching	87
Brian Hudson: Global Perspectives in the Mathematics Classroom	87
Tadasu Kawaguchi: Mathematical Thoughts Being Latent in Various Artistic Activities	89

Diana Schultz: PRIMITE—Projects in Real-Life Integrated Mathematics in Teacher Education	91
Joop van Dormolen: Values of Texts for Learning Mathematics for Real Life	94
How Autonomous is the Mathematics Teacher?	97
Dianne E. Siemon: How Autonomous is the Teacher of Mathematics?	97
Paul Ernest: The Impact of Beliefs on the Teaching of Mathematics	99
Kurt Kreith: The Recruitment and Training of Master Teachers	101
John Suffolk: The Role of the Mathematics Teacher in Developing Countries	103
Ethnomathematics and Schools	105
Gloria F. Gilmer: World-wide Developments in Ethnomathematics	105
Randall Souviney: The Indigenous Mathematics Project: Mathematics Instruction in Papua New Guinnea	106
Eduardo Sebastiani Ferreira: The Genetic Principle and the Ethnomathematics	110
Social Needs and Reforms in Mathematics Education	111
Feiyu Cao: School Mathematics Education Should Suit the Needs of Social Development	111
Fidel Oteiza and Nadja Antonijevic: On the Light of Present and Future Needs, are we Teaching the Proper Mathematics? The Case of Chile	114
Teresa Smart and Zelda Isaacson: "It was Nice Being Able to Share Ideas": Women  Learning Mathematics	116
George Malaty: ICMI and the Crisis of Mathematics Education: What Kind of Reform is Needed?	118
Educational Institutions and the Individual Learner	121
Individual and Social Learning Motivations	121
Anne-Nelly Perret-Clermont and Maria-Luisa Schubauer-Leoni: The Social Construction of Meaning in Math Class Interactions	121
Timothy E. Erickson: Cooperative Learning in Mathematics: A Way to Engage All Students	123
Albrecht Abele: Socialization and Learning Mathematics	124
Cultural Influences on Learning	126
Analucia Dias Schliemann and Nadja Maria Acioly: Numbers and Operations in Everyday Problem Solving	126
Frederick K. S. Leung: The Chinese Culture and Mathematics Learning	128
Martin R. Hoffman and Arthur B. Powell: Mathematical and Commentary Writing:	00 100
Vehicles for Student Reflection and Empowerment	131
Are Girls Underprivileged Around the World?	124
	134
Gila Hanna: Girls and Boys About Equal in Mathematics Achievement in Eighth Grade:  Results From Twenty Countries	134
Erika Kuendiger: Mathematics—A Male Subject?!	137
Frank J. Swetz: Cross-Cultural Insights Into the Question of Male Superiority in	-73-40.5
Mathematics: Some Malaysian Findings	139

Societal Determinants of Learning	140
Joan Bliss, Ruffina Guttierez, Vasilios Koulaidis, Jon Ogborn, and Haralambos N. Sakonidis:	
A Cross-Cultural Study of Children's Ideas About What is Really True in Four Curricula Subjects: Science, Religion, History, and Mathematics	141
	143
Gustav Adolf Lörcher: Learning Mathematics in a Foreign Language	146
Ali Rejali: Lack of Interest of Students for Studying Mathematics	147
Ali Rejali: Lack of Interest of Students for Studying Mathematics	et line
The Social Arena of the Mathematics Classroom	148
The Social Arena of the Mathematics Classroom	149
Josette Adda: The Mathematics Classroom as a Microsociety	
Tom Cooper: Negative Power, Hegemony, and the Primary Mathematics Classroom:  A Summary	150
Andrea L. Petitto: The Structure of Mathematical Discourse Among Teachers and Children	154
Torry Wood: Whole Class Interaction as the Negotiation of Social Contexts Within	ni • 55
Which to Construct Mathematical Knowledge	155
Learning Under Difficult Conditions	157
Learning Under Difficult Conditions	
Marilyn Frankenstein and Arthur B. Powell: Mathematics Education and Society:  Empowering Non-Traditional Students	
Françoise Cerquetti-Aberkane: Teaching Mathematics in Special Classes for Children With	160
Serious Difficulties in France	
Nick Taylor: "Let Them Eat Cake"—Desire, Cognition, and Culture in Mathematics Learning	101
Mathematics Education in Multi-Cultural Contexts	163
Raymond A. Zepp: New Direction in Research on Language in Mathematics	163
Ina Kurth: Learning Mathematics in a Foreign Language	165
Helen Watson: Mathematics Education From a Bicultural Point of View	1/1
Norma C. Presmeg: Mathematics Education and Cultural Continuity	172
Ethnomathematical Practices	
	174
Salimata Doumbia: Mathematics in Traditional African Games	174
Sergio Roberto Nobre: The Ethnomathematics of the Most Popular Lottery in Brazil:	175
The "Animal Lottery"	177
Nigel Langdon: Cultural Starting Points	
Social Construction of Mathematical Meaning  Paul Cobb: Children's Construction of Arithmetical Knowledge in Social Context	181
Paul Cobb: Children's Construction of Arithmetical Knowledge in Social Context	181
Erna Yackel: The Negotiation of Social Context for Small-Group Problem Solving	
in Mathematics	105
Stieg Mellin-Olsen: Creative Uses of Mathematics in Social Contexts	184
The Magning of Mothematical Tacks for Punils and Teachers	186
Jan Waszkiewicz and Agnieszka Wojciechowska: The Future Cultural Role of Mathematics and its Impact on Math Education	187

Hearing 1: Which and Whose Interests are Served by Math	ematics Education?
Hearing 2: How Does Mathematics Education Relate to D	
Hearing 3: Do Mathematics Educators Know What they ar	
Hearing 4: What are the Challenges for ICMI in the Next I	
Hearing 5: What can we Expect From Ethnomathematics?	

spect, he called for the same reform in the mathematical education of women as in that of men.

Changes in all Mathematical and Scientific Education, Particularly in Elementary Schools

It is not possible to discuss here the question of whether changes in this area really took place. One can only emphasize Klein's great efforts to bring about changes in the law, in examination requirements, and curricula as well as in teacher training as the essential prerequisites for effective changes in classroom practice. Klein explained the relevant demands of the Teaching Commission in three speeches: on 21 May 1909, on 27 May 1910, and on 7 April 1911. In the first two he spoke about the existing institutions of secondary education. The third speech was dedicated exclusively to elementary schools. This special emphasis on elementary education was unusual for a university professor at that time. Klein criticized the encyclopedic training of teachers for elementary schools, asked for the introduction of courses for theoretical training, and for financial means to be made available for improving it. Klein's demands for scientifically trained teachers for elementary schools surpassed the ideas of many of his contemporaries. Klein's views corresponded in this respect to those of the German social democrats, although he was a loyal subject to the existing state. The ideas of Klein remind us of the demands of progressive bourgeois pedagogues, which were also utopian under the existing social conditions.

The activities of the Teaching Commission and Klein's function as vicepresident ended with the breakup of the German empire, but the results of their work were able to be preserved. Klein's interests in mathematical and scientific education and in education generally were not dependent on the political situation. He wrote a letter to the Ministry only a short time after the November revolution offering his help in the planning of education. The Ministry of Science, Art, and National Education answered gratefully in a letter of 18 January 1919. Among Klein's papers there is preserved a draft of a lecture entitled "Mathematical instruction at the various types of schools (and debate)." It dates from 7 January 1919 and shows his continuing determination to accomplish the demands for reform under the new regime. For this purpose he formulated a number of theses in his draft:

 Comprehensive public education should form an ideal unity, its separate areas being adequately proportionate to each other.

By this, Klein wanted to make clear the relationship between pedagogic and subject-specific instruction, between general and vocational schools.

Klein saw the necessity for promoting such subjects as philosophy, psychology, and for creating new chairs of general pedagogics and of didactics in the various subjects of instruction at the universities.

 New ideas were to be put into practice to teach future research scientists and teacher students separately.

 Klein insisted on doing everything possible to achieve higher appreciation for mathematics and science at schools and in public.

In promoting those aims, a new institution was founded on 6 January 1921: the "Association of German Mathematical Clubs and Societies."

#### References

Stenographische Berichte über die Verhandlungen des preußischen Herrenhauses, 1899/1900 bis 1917/18. Berlin.

Tobies, R. (1981). Felix Klein. Biographien hervorragender Naturwissenschaftler, Techniker und Mediziner, 50. Leipzig: B. G. Teubner.

Tobies, R. (1989). Felix Klein als Mitglied des preußischen "Herrenhauses"—Wissenschaftlicher Mathematikunterricht für alle Schüler—auch für Mädchen und Frauen. Der Mathematikunterricht, 35, 1, 4-12.

The Teaching of Geometry in Italian High Schools During the Last Two Centuries: Some Aspects Related to Society

Emma Castelnuovo

My subject concerns Italian high schools during the last two centuries. As this period is very long, I will emphasize only those points which, in my opinion, are rather original.

First of all I will begin talking about a French book of the 18th century which had a great influence on our teaching of geometry. The book is *Eléments de géométrie* by A. C. Clairaut, the great mathematician and astronomer; it was written in 1741. The idea of Clairaut was to present geometrical properties in such a way, that beginners would be stimulated to investigate. He says, in his preface, that beginners are not able to follow a book like Euclid's Elements, starting with axioms and abstract properties. He bases his work on examples taken from agriculture, the economy of his country being essentially agricultural: the problem of how to measure fields of different shapes,

But Clairaut's Elements never influenced the teaching of mathematics in France. On the contrary, this book, translated into Italian, was used for many years as a textbook in some technical schools of Lombardia, a region in northern Italy. Without any doubt the book was used because of a strange coincidence: The governors of Lombardia thought that Clairaut's book would be very suitable for the technical-agricultural

schools because many examples were connected with the measurement of fields. It is interesting to observe that Clairaut had foreseen this misunderstanding; in his preface he says, with humor: "I do hope that people do not think that this book has been written for students of agriculture; the problems of measuring fields only represent a stimulus to investigate further." However, Clairaut's Elements, interpreted rightly or wrongly, were widely used in our country in the first half of the last century.

The unification of Italy in 1861 led to the establishment of national curricula in our schools. The curricula of mathematics in secondary schools were published in 1867 by three distinguished mathematicians: Cremona, Betti, Brioschi. The ideas inspiring these curricula are clearly described by their preliminary directives; they say: "The fundamental aim of mathematics is to accustom pupils to reasoning and deduction." It is clear that the application of mathematics were excluded. I would like to underline that, even without an explicit declaration, these curricula were conceived for students of a high social level. But a very unusual fact happened in Italy: In 1881, that is 15 years after the publication of new curricula, a very open-minded Minister of Education, a doctor named Guido Baccelli, declared that the curriculum of geometry was too abstract for pupils 11 to 14 years old. He succeeded in convincing the mathematicians to introduce into the junior secondary school the so-called "Intuitive Geometry." He thought, particularly, of lower social level children. Thanks to this Minister, Italy was the first country to introduce Intuitive Geometry. But this new course was not very original: It reproduced the senior course of geometry leaving out the traditional proofs.

At the same time, curricula of senior schools have always been inspired by Euclid, even if, at the beginning of this century, some mathematicians declared the absurdity of such a purism in a modern society. I would like to quote the declaration of Guido Castelnuovo, pronounced in 1912 during a national congress on the teaching of mathematics. He says: In our schools we drive students to idolize a perfection which is illusory, instead of encouraging them to work with approximations. We must accustom them to compare theory with practise

in order to prepare people able to participate in the life of our

But voices like this always remained unheard at the

political level.

After the last war many initiatives flourished on education. For what concerning the teaching of geometry in junior secondary schools, a critical study of Clairaut's old book gave brilliant ideas. The examples on fields of different shapes and their measurement were replaced by up-to-date examples and problems, and geometry was strictly connected to the other branches of mathematics in order to investigate practical and theoretical problems. In 1979 a new reform of the first secondary cycle officially recognized the value of these experiments. A geometry motivated by various real problems became a part of a brilliant and widespread course of mathematics. A "dynamic"

course whose principal aim is to sensitize pupils to the function concept.

I have to point out that teachers have always had full freedom in their teaching. It is this freedom, perhaps, that saved us from the so-called "modern mathematics."

When, in the 60s, most countries were introducing at all levels mathematics inspired by set theory, Italy was continuing with its curricula and methodology, completely oblivious to a fashion which was invading the world. Why? Some foreign mathematicians say that our behavior was due to the influence that Galileo's thought has had on Italian people: Galileo never proceeded without experimenting or without foreseeing the result which one experiment could produce. I really should like to think that this interpretation reflects the truth!

#### Some Reflections on the Role of Associations in Mathematics Education

Michael H. Price

My interest in this topic springs from some research I am currently undertaking to produce a commissioned history of the Mathematical Association in England, from 1871. This project is developing along the lines of a case study in a growing field of educational inquiry: the history of the curriculum. Investigating the role of associations generally in the shaping of curriculum is one aspect of curriculum history. Thus, my interests now embrace not only the Mathematical Association but all forms of association having a significant stake in English mathematics education, as well as comparisons across the curriculum, and particularly in the case of science education. There may also be some interesting comparisons to be made with other countries, where national patterns of educational organization and curriculum development may vary considerably. Furthermore, the patterns in one country may change dramatically over a comparatively short time, as is the case in England under the present Conservative Government.

In relation to mathematics education, this short paper will only consider the following aspects of the development of associations and their roles:

- (1) Variety of forms;
- (2) A framework for investigating associations;
- (3) Growing complexity.

## Variety of Forms

The roots of the Mathematical Association are to be found in the establishment of the Association for the Improvement of Geometrical Teaching (AIGT) in 1871. This was the first of the academic *subject*